



Original Article

## Effect of Eu Doping on Structural, Optical and Magnetic Properties of BiFeO<sub>3</sub> Materials

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**Abstract:** Bi<sub>1-x</sub>Eu<sub>x</sub>FeO<sub>3</sub> (BEFO) ( $x = 0.00 \div 0.10$ ) materials were prepared by sol-gel method. The crystal structural, Raman scattering, magnetic and optical properties of BEFO were investigated by X-ray diffraction (XRD), Raman scattering spectroscopy, magnetic hysteresis (M-H) loops and fluorescence spectroscopy (FL), respectively. Obtained results of the characterization showed that Eu-doping affected structural, optical and magnetic properties of BFO materials. All samples were crystallized in the rhombohedral structure with  $R_{3C}$  space group with crystal lattice parameters of  $a = 5.585 \text{ \AA}$ ,  $c = 13.832 \text{ \AA}$  and the average crystal size of  $L_{XRD} = 581 \text{ \AA}$  for BFO materials whereas the  $a$ ,  $c$  and  $L_{XRD}$  of Eu-doped samples decrease with the increasing of Eu<sup>3+</sup> concentration. The analysis result of Raman scattering spectroscopy showed that the position of the characteristic peak for Bi-O covalent bonds shifts toward higher frequency when Eu<sup>3+</sup> concentration increases, confirming the doping substitution of Eu<sup>3+</sup> ions into Bi-sites. Fluorescence spectra showed the enhancement of characteristic emission peaks with the increase of Eu concentration. All samples exhibited weak ferromagnetic behaviour with saturation magnetization of  $M_s = 0.006 \text{ emu/g}$  and remnant magnetization of  $M_r = 0.004 \text{ emu/g}$  for BFO materials. The value of  $M_s$  and  $M_r$  of Eu-doped BFO increases compared to those of undoped-BFO. The origin of ferromagnetism and fluorescence improvement has been discussed.

**Keywords:** Fluorescence, ferromagnetic, Eu-doped, X-ray, Raman.

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## 1. Introduction

Multiferroic materials are well known to contain ferroelectric and ferromagnetic (antiferromagnetic) orders simultaneously and exhibit ferroelastic and magnetoelectric (ME) effect in the same structure phase [1]. These materials have found broad applications in electronic devices such as information storage, memory, sensor, and in ultrasonic technologies. The multiferroic materials are very rare in nature because of the competition between the ferromagnetic and the ferroelectric orders. BiFeO<sub>3</sub> (BFO) was found to be one of the few multiferroic materials where the antiferromagnetic order (with Néel temperature  $T_N = 643$  K) and the ferroelectric order (with Currie temperature  $T_C = 1100$  K) coexist [2, 3]. Recent studies have showed that the optical properties of doped BFO materials can be applied for the next generation of smart materials. At room temperature, BFO crystallizes in a rhombohedral structure with  $R_{3C}$  space group [4, 5]. The rhombohedral structure may be obtained from a cubic parent perovskite by the rotation of the oxygen octahedra around the (111) direction and the displacement of Bi<sup>3+</sup> and Fe<sup>3+</sup> cations along the same  $c$  direction [6]. Fe<sup>3+</sup> ions are located in the distorted oxygen octahedra, while Bi<sup>3+</sup> ions, occupying the dodecahedron positions are strongly shifted from the central position towards one of Fe<sup>3+</sup> ions due to the electron lone pair of Bi<sup>3+</sup> effect.

Recently, some studies have shown the influence of impurity element, impurity concentration and fabrication conditions such as temperature and pressure on crystal structure and physical properties of the host BFO materials [7]. The studies indicated the strong dependence of magnetic properties on nanoscale structure [8]. For example, while BFO presents anti-ferromagnetic behaviour with G-type cycloid spin configuration with a period of 62 nm, BFO doped with rare earth (RE) ion exhibits an enhancement of both ferromagnetic and optical properties which are important requirement for the next generation of multifunctional devices. Some recent reports showed the effect of Eu<sup>3+</sup> doping on the characteristics of BiFeO<sub>3</sub> powders produced by conventional techniques such as hydrothermal process and sol-gel method [9-13]. Even if the magnetic behaviours of Eu-doped BFO have been thoroughly analyzed, very few data regarding fluorescence has been reported.

Herein, we studied the effect of Eu<sup>3+</sup> doping on the structural, magnetic and optical properties of BFO materials. In particular, the fluorescence data are carefully analyzed to show the enhancement in optical properties of the doped samples, which is beneficial for the fabrication of next-generation multifunction devices.

## 2. Experiment

Pure BiFeO<sub>3</sub> and Eu<sup>3+</sup>-doped BiFeO<sub>3</sub> materials were synthesized by the sol-gel method. The initial chemicals were: Bi(NO<sub>3</sub>)<sub>3</sub>.5H<sub>2</sub>O (Sigma-Aldrich, 98%), Fe(NO<sub>3</sub>)<sub>3</sub>.9H<sub>2</sub>O (Sigma-Aldrich, 98%), Eu(NO<sub>3</sub>)<sub>3</sub>.6H<sub>2</sub>O (Sigma-Aldrich, 99,9%), ethylene glycol C<sub>2</sub>H<sub>6</sub>O<sub>2</sub> (Sigma-Aldrich, 98%), and citric acid HOC(COOH)(CH<sub>2</sub>COOH)<sub>2</sub> (Sigma-Aldrich, 98%). Firstly, Bi(NO<sub>3</sub>)<sub>3</sub>.5H<sub>2</sub>O, Fe(NO<sub>3</sub>)<sub>3</sub>.9H<sub>2</sub>O and Eu(NO<sub>3</sub>)<sub>3</sub>.6H<sub>2</sub>O were dissolved in 35 ml of citric acid solution. The solution was then magnetically stirred at temperature 60 °C for 45 minutes to obtain homogeneous solutions. Then, by heating the solutions up to temperature of 100 °C for 3 hours, water in the solution were evaporated and a wet gel was formed. The gel was dried at 130 °C for 4 hours to achieve a condensed gel. Finally, the dry gel was annealed at temperature of 800 °C for 7 hours to get BFO powder materials.

The structural, magnetic and optical properties of all samples were investigated by using X-ray diffraction (Equinox 5000, Cu-K $\alpha$  radiation), Raman scattering (LabRAM HR Evolution,  $\lambda = 532$  nm), magnetization hysteresis loops ( $M-H$ , Lake Shore Cryotronics, 7404 VSM), and fluorescence emission spectroscopy (iHR550, Horiba,  $\lambda = 266$  nm).

### 3. Results and Discussion

The phase formation and crystalline structure of  $\text{Bi}_{1-x}\text{Eu}_x\text{FeO}_3$  materials ( $x = 0, 0.025, 0.05, 0.075,$  and  $0.10$ ) were investigated by XRD measurement. The XRD patterns of all samples are shown in Figure 1. The refinement of these patterns following the standard Cards JCPDS No. 71-2494 revealed that all samples exhibit rhombohedral structure. The main characteristic diffraction peaks belong to the (012), (104), (110), (006), (202), (024), (116), (122), (018), and (300) crystalline planes, as shown in Figure 1a. The XRD of BFO pure and Eu-doped  $\text{BiFeO}_3$  samples show that  $\text{Eu}^{3+}$  ions are well incorporated into the BFO crystal lattice. Figure 1b shows a comparison of the positions of the (012), (104), and (110) peaks, which may depict the effect of Eu-doping on the crystalline structure of BFO. As it is seen, the corresponding peaks of the Eu-doped samples shift toward larger  $2\theta$  values compared to those of BFO. From XRD data, the crystal lattice parameters ( $a$  and  $c$ ) and the average crystal size ( $L_{\text{XRD}}$ ) have been determined by using the UnitCell software and Debye Sherrer's formula, and results are shown in Table 1. As seen in Table 1, the BFO pure sample has crystal lattice parameters of  $a = 5.585 \text{ \AA}$ ,  $c = 13.832 \text{ \AA}$  and the average crystal size  $L_{\text{XRD}} = 58.1 \text{ nm}$ . It is also seen that the crystal lattice parameters and the average crystal size of Eu-doped samples decrease when the concentration of Eu increases. This observation can be easily understood considering the smaller ionic radius of  $\text{Eu}^{3+}$  ( $1.07 \text{ \AA}$ ) compared to that of  $\text{Bi}^{3+}$  ( $1.17 \text{ \AA}$ ). When the  $\text{Eu}^{3+}$  ions are substituted into Bi-sites, the crystal lattice of the sample was a little bit contractive, resulting the decrease of the Bi/Eu-O bond length.. Furthermore, the  $\text{Eu}^{3+}$  ion with the small ionic radius is not large enough to fill 12-sided cavity created by the  $\text{BO}_6$  octahedron causing the  $\text{BO}_6$  octahedron to rotate, which reduces the 12-sided cavity volume. So, the Eu-doped  $\text{BiFeO}_3$  samples with larger Eu ion concentrations, the rotation of  $\text{BO}_6$  octahedron is significant leading to significant reduction of both the crystal lattice parameters of  $a$  and  $c$ . This is maybe the reason why the average crystal size  $L_{\text{XRD}}$  decreased, as shown in Table 1. The report of Park *et al.* [14] and Surdu *et al.* [15] also indicated that the crystal lattice parameters changed due to the difference in ionic radius of rare-earth ions and  $\text{Bi}^{3+}$  ions.

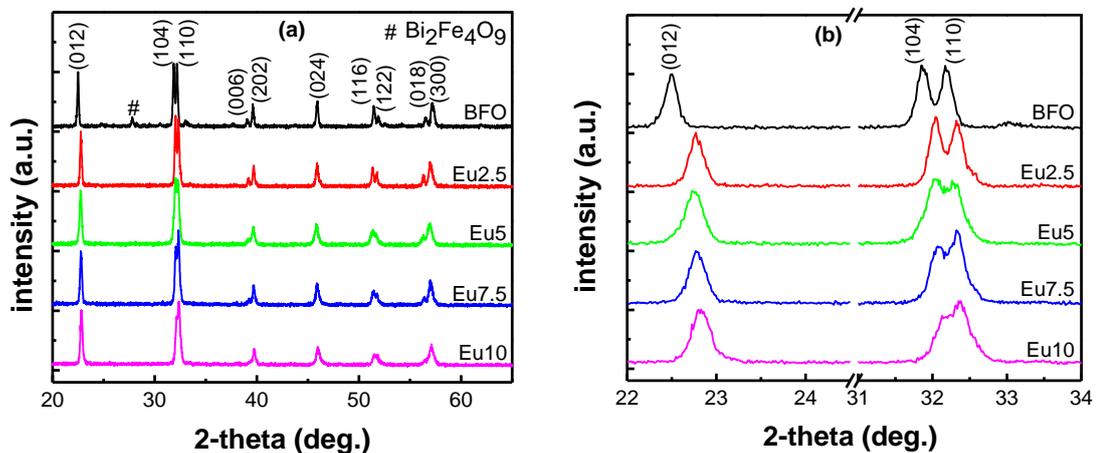


Figure 1. a) X-ray diffraction patterns of pure BFO and Eu-doped BFO materials; b) Magnification of (012), (104), and (110) diffraction peaks.

Table 1. The crystal lattice parameters ( $a$  and  $c$ ) and the average crystal size  $L_{XRD}$  of BFO and Eu-doped BiFeO<sub>3</sub> samples.

Samples	$a$ (Å)	$c$ (Å)	$L_{XRD}$ (nm)
BFO	5.585	13.832	58.1
Eu2.5	5.572	13.826	56.7
Eu5	5.570	13.820	49.4
Eu7.5	5.562	13.810	46.2
Eu10	5.555	13.787	43.9

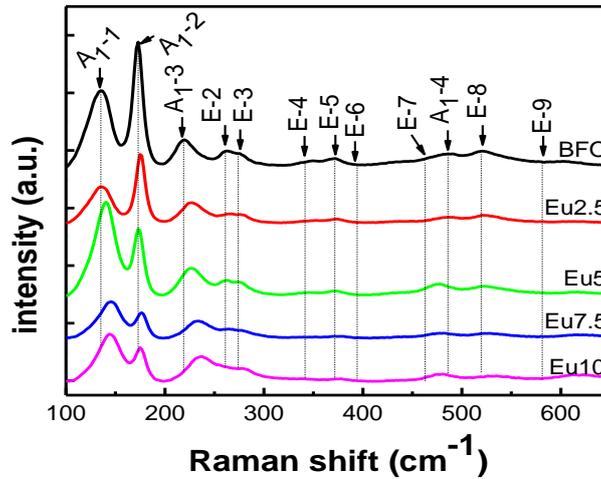


Figure 2. Raman scattering spectra of pure BFO and Eu-doped BFO materials.

Table 2. Raman modes observed and assigned by various research and Raman modes for BFO and Eu-doped BiFeO<sub>3</sub> samples.

Modes	Position of Raman modes (cm <sup>-1</sup> )					
	Yang et al., [18]	BFO	Eu2.5	Eu5	Eu7.5	Eu10
A <sub>1</sub> -1	139	134	135	140	144	145
A <sub>1</sub> -2	171	173	175	173	176	177
A <sub>1</sub> -3	217	218	226	227	233	236
E-2	260	228	237	241	261	261
E-3	274	260	271	275	276	280
E-4	306	270	275	279	283	284
E-5	344	348	350	344	342	338
E-6	368	371	374	373	376	376
E-7	430	467	471	444	443	411
A <sub>1</sub> -4	468	482	485	476	478	478
E-8	520	523	525	524	528	531
E-9	611	589	595	611	621	621

Raman scattering spectra of BFO and Eu-doped BiFeO<sub>3</sub> are shown in Figure 2. According to the group theory, 13 Raman active modes could be expected for the rhombohedral BFO structure with the  $R_{3C}$  space group ( $\Gamma = 4A_1 + 9E$ ) [16, 17]. However, not all modes could be clearly observed at room

temperature. In the analysis of Raman scattering spectra for all samples, the position of Raman active modes for all samples are fitted by the Gaussian function, and results are presented in Table 2. As one can see in Table 2, for the Eu-doped BFO samples, there is a shift towards the higher frequencies in the position of the  $A_1-1$ ,  $A_1-2$ ,  $A_1-3$ ,  $E-2$ ,  $E-3$ ,  $E-4$ ,  $E-6$ ,  $A_1-4$ ,  $E-8$ ,  $E-9$  compared to the situations in the BFO sample. Previous studies have also shown that both the  $A_1$  modes and the  $E$  modes at low frequencies are characteristic modes for the Bi-O covalent bonds, while other  $E$  modes at high frequencies are characteristic for the Fe-O bonds [9, 16]. Therefore, the  $A_1-1$ ,  $A_1-2$ ,  $A_1-3$ ,  $E-2$ ,  $E-3$ ,  $E-4$ ,  $E-6$  and  $A_1-4$  modes are found characteristic for the Bi-O covalent bonds and the  $E-8$ ,  $E-9$  modes are characteristic for the Fe-O bonds. The observed shift of the positions of  $A_1-1$ ,  $A_1-2$ ,  $A_1-3$ ,  $E-2$ ,  $E-3$ ,  $E-4$ ,  $E-6$ ,  $A_1-4$  modes showed that the  $\text{Eu}^{3+}$  ions are substituted into the Bi-sites. These results are consistent with the XRD results, confirming the substitution doping of  $\text{Eu}^{3+}$  ions into Bi-sites.

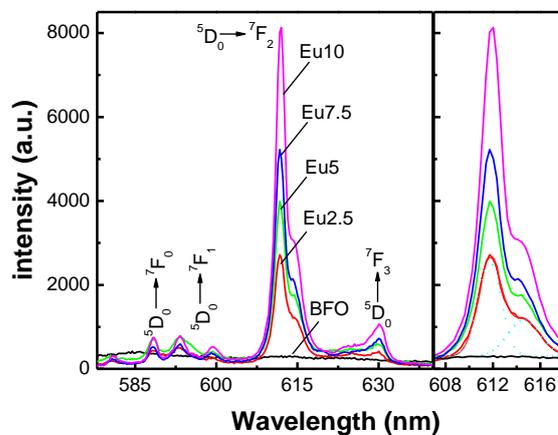


Figure 3. Fluorescence spectra of pure BFO and Eu-doped BFO materials.

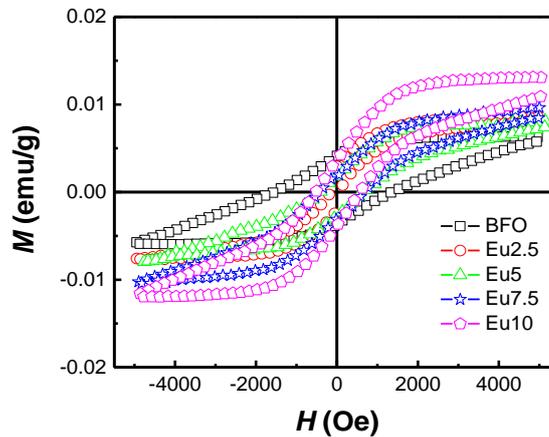


Figure 4. Magnetic hysteresis loops of BFO and Eu-doped  $\text{BiFeO}_3$  materials.

Figure 4 shows the magnetic hysteresis loops of a pure BFO and Eu-doped BFO samples measured at room temperature. It is obvious that all samples exhibited weak ferromagnetic behaviour. The BFO sample has a saturation magnetization of  $M_s = 0.006$  emu/g and a remnant magnetization  $M_r$

= 0.004 emu/g. For the Eu-doped BFO samples, the  $M_s$  value increases from 0.008 to 0.013 emu/g while the  $M_r$  value slight changes when concentration of  $\text{Eu}^{3+}$  ions increase from 0.025 to 0.10, respectively. These results can be explained from the following considerations. The substitution of the  $\text{Eu}^{3+}$  ions into  $\text{BiFeO}_3$  crystal lattice along with high temperature annealing of samples creates oxygen vacancies and lattice defects thereby contributing to the enhancement of the magnetization. In addition, the increase in  $\text{Eu}^{3+}$  concentration affects the spin spiral structure, most likely by a perturbation of the super-exchange interactions between localized Eu 4*f* and Fe 3*d* electrons. Some previous studies have also showed that the super-exchange interactions between localized RE 4*f* and Fe 3*d* electrons contributed in the enhancement of the magnetization of RE-doped  $\text{BiFeO}_3$  materials [20-22].

#### 4. Conclusion

In summary, both the pure  $\text{BiFeO}_3$  and Eu-doped  $\text{BiFeO}_3$  materials were successfully synthesized by the sol-gel method. XRD and Raman scattering investigation showed the substitution doping of  $\text{Eu}^{3+}$  ions into the Bi-sites in the host  $\text{BiFeO}_3$  lattice. The most pronounced ferromagnetic behaviour was observed for Eu-doped  $\text{BiFeO}_3$  samples with  $\text{Eu}^{3+}$  concentration of 10% molar which exhibited a saturation magnetization of  $M_s \sim 0.013$  emu/g. This is most likely ascribed to the disorder of the super-exchange interactions between localized Eu 4*f* and Fe 3*d* electron. This study indicated a possibility to improve magnetic behaviour of  $\text{BiFeO}_3$  using rare earth metal substitution into the A-site of the perovskite structure. In addition, the substitution of  $\text{Eu}^{3+}$  ions into Bi-sites of the host BFO materials enhanced the photoluminescence of the materials. This is a good sign for the search for new materials that are suitable for making next-generation multifunction devices.

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